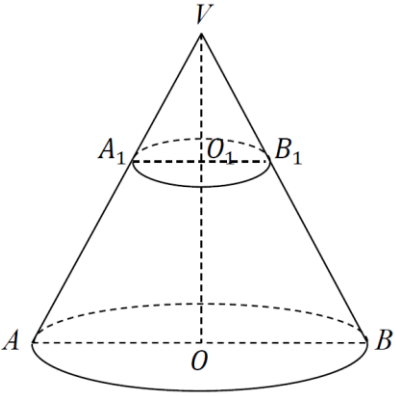


| No. | Items | Score | | |
|-----|---|---|---------------------------------|-------------|
| 1. | Fill in the boxes with two consecutive integers, so that the statement becomes true. $\square < \sqrt[3]{-17} < \square .$ | L 0 1 2 | L 0 1 2 | |
| 2. | Consider the function $f: \left[0; \frac{\pi}{2}\right] \rightarrow \mathbb{R}, f(x) = \cos x$. Fill in the box with one of the expressions “monotonically decreasing” or “monotonically increasing”, so that the statement becomes true. “The function f is <input data-bbox="517 539 1342 607" type="text"/> .” | L 0 2 | L 0 2 | |
| 3. | On the picture the right circular cone with the altitude $VO = 6$ cm is represented. The cone is cut by a plane parallel to the base at the distance of 2 cm from the vertex V . Write in the box the length of the radius of the circle from the cross-section, if it is known that the length of the radius from the base is equal to 15 cm. $O_1B_1 = \square$ cm. |  | L 0 2 | L 0 2 |
| 4. | Calculate the value of the expression $\log_2 5 + 2 \log_{\frac{1}{4}} 20 + 32^{\frac{1}{5}}$. <i>Solution:</i> <i>Answer:</i> _____ | L 0 1 2 3 4 | L 0 1 2 3 4 | |
| 5. | Consider $z = \frac{(3+i)^2}{2i}$, where $i^2 = -1$. Determine \bar{z} . <i>Solution:</i> <i>Answer:</i> _____ | L 0 1 2 3 4 5 | L 0 1 2 3 4 5 | |

6.

Solve in the set \mathbb{R} the inequality $\left(\frac{64}{27}\right)^{x-4} \geq \left(\frac{9}{16}\right)^{6+x}$.

Solution:

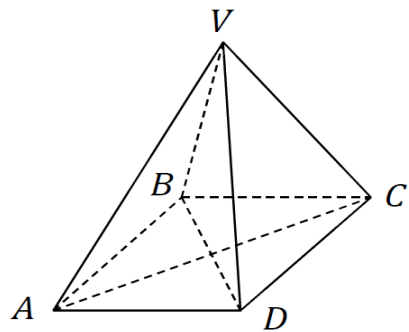
| | |
|---|---|
| L | L |
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 4 |
| 5 | 5 |

Answer: _____.

7.

Consider the regular square pyramid $VABCD$, where VAC is a right-angled triangle with the legs of 6 cm. Determine the volume of the pyramid.

Solution:



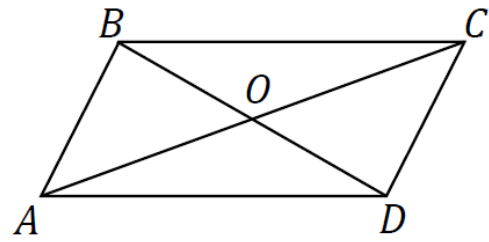
| | |
|---|---|
| L | L |
| 0 | 0 |
| 1 | 1 |
| 2 | 2 |
| 3 | 3 |
| 4 | 4 |
| 5 | 5 |
| 6 | 6 |

Answer: _____.

10.

Consider the parallelogram $ABCD$, where $AB = 13$ cm, $BD = 16$ cm and O is the point of intersection of the diagonals. Determine the perimeter of the parallelogram $ABCD$, if $m(\angle AOB) = 60^\circ$.

Solution:



L
0
1
2
3
4
5
6

L
0
1
2
3
4
5
6

Answer: _____.

Annex

$$\log_a b + \log_a c = \log_a(b \cdot c), \quad a \in \mathbb{R}_+^* \setminus \{1\}, \quad b, c \in \mathbb{R}_+^*$$

$$\log_a b - \log_a c = \log_a \frac{b}{c}, \quad a \in \mathbb{R}_+^* \setminus \{1\}, \quad b, c \in \mathbb{R}_+^*$$

$$\log_a b^c = c \log_a b, \quad a \in \mathbb{R}_+^* \setminus \{1\}, \quad b \in \mathbb{R}_+^*, \quad c \in \mathbb{R}$$

$$\log_{a^c} b = \frac{1}{c} \log_a b, \quad a \in \mathbb{R}_+^* \setminus \{1\}, \quad b \in \mathbb{R}_+^*, \quad c \neq 0$$

$$C_n^m = \frac{n!}{m!(n-m)!}, \quad 0 \leq m \leq n$$

$$(x^\alpha)' = \alpha x^{\alpha-1}, \quad \alpha \in \mathbb{R}$$

$$(\ln x)' = \frac{1}{x}$$

$$\int x^\alpha dx = \frac{x^{\alpha+1}}{\alpha+1} + C, \quad \alpha \in \mathbb{R} \setminus \{-1\}$$

$$c^2 = a^2 + b^2 - 2ab \cos \varphi$$

$$\mathcal{V}_{\text{pyramid}} = \frac{1}{3} \mathcal{A}_b \cdot H$$